## 1. THE SLABS

Nowadays, reinforced concrete slabs have become very common in the spanish construction market. Although, the traditional beam systems are still very used, other technologies gained the upper hand.

If we get a closer look at what is the trend around the world, beam slabs are still used in the countries where materials costs are higher than labour costs.

On the other hand, richer and industrialized countries, use deck plates.
Reinforced concrete slabs:

1. Are very solid. Thanks to side deformation prevention, they can't deform and the thickness can be reduced.
a. Thickness reduction allows the economisation of materials
b. Massing reduction, allows the maximisation of the ground surface exploitation, which is very important cost item.
2. Does not need beams:
a. They allow the reduction of the volumetric footprint of the deck
b. They avoid the scaffolding of the beams
c. They facilitate the passage of installations, significantly reducing installation times
3. They are reinforced with meshes and straight bars :
a. Reduction of the iron reinforcements costs. Wought iron is more expensive
b. Meshes and straight bars are easier and faster to install
c. It is possible to use pre-fabricated reinforced systems, in order to make the work faster (like BAMTEC layers of reinforcements)
4. They have an excellent fire and acoutic behaviour, thanks to their mass.

If we read the upper points, it looks like slab structures does not have any disadvantage, but, on the contrary, they also have some weak points that limit their use in respect to other more efficient methods:

They are massive structures:

- They consume an high quantity of concrete
- They are very heavy: there are large spans between the pillars, but the self-weight prevails and the result is very expensive

2. They are not flexible:

- They can't be calculated as the classic structures
- They need low structures



## 2. LIGHTENED SLABS

### 2.1. ADVANTAGES

They are structures with all the characteristics and strength points of standard slabs, but without their selfweight:

1. Limited volumes
2. No beams
3. Concrete is less expensive
4. Larger spans
5. Optimization of vertical structures
6. Reduced foundation load
7. Reduced excavation load


### 2.2. RETICULAR SLABS

The slabs mantain their bidirectional structure and create an orthogonal grid through the installation of disposable blocks (in concrete or terracotta) or reusable (in plastic or fibreglass). Massive capitals are embeded in the pillars for the punching.

### 2.2.1. ADVANTAGES

The advantages this type of solution offer, are multiple

1. They are slabs without beams
2. The quantity of concrete needed is reduced
3. They are very light
4. Less steel used

### 2.2.2. WEAK POINTS

These structures has also some disadvantages:

1. In comparison to reticular slabs, they consume more concrete and weight more.
2. They consume also more steel


### 2.2.3. CONCLUSIONS

This type of solution is ideal for narrow spans and low weight slabs. Apart from these applications they become less competitive.

## LIGHTENED SLABS

Hollow articles are embeded in the pour. Usually they are made of cubic shaped polystyrene or plastic. Blocks remain embeded in the pour and create a grid of ribbings, which are enclosed between two massive upper and lower slabs.

## ADVANTAGES

This solution is more efficient than most reticular slabs
5. The lower slab makes it perfect for all intents and purposes
6. The same thickness of full slabs can be mantained
7. They guarantee lightness and concrete savings
8. They can be reinforced in the same way as massive slabs
9. Steel is reduced
10. Great seismic behaviour
11. Great fire behaviour (up to REI 240')
12. Does not need a false ceiling

### 2.2.4. WEAK POINTS

## Even these structures have some disadvantages

3. In comparison to reticular slabs they consume more concrete and weight more
4. They consume more steel

### 2.2.5. CONCLUSIONS

3. This type of solution is ideal for narrow spans and low weight slabs. Apart from these applications they become less competitive.

On the contrary, it is extremely competitive if compared to a full slab, especially with a thickness from 28 to 60 cm and spans from 8 to 14 m .

### 3.1. LIGHTENED SLABS WITH HOLLOW ARTICLES IN PLASTIC

### 3.1.1. General Characteristics

Since 10-15 years ago, lightened slabs were created through the use of cubic blocks in polystyrene.
This contruction method had some disadvantages:

1. Blocks were fragile and suffer from weatherings
2. Blocks were bulky and did not facilitate worksite logistics
3. It was not easy to block them during the pour

During recent years a new construction methods has arrived in the market. This solution allows the overrun of these limitations.


They are recycled polypropilene formworks, $52 \times 52 \mathrm{~cm}$ with variable height. They can be "single", or "double", by putting together two "single".


Figura 1 - Plastic lightening "single"type.


Figura 2 - Plastic Lightening "double" type

## PLASTIC LIGHTENINGS HEIGHTS « DOUBLE »

| H23 cm | H 37 cm |
| :--- | :--- |
| H 26 cm | H 38 cm |
| H29 cm | H 40 cm |
| H30 cm | H 41 cm |
| H32 cm | H 44 cm |
| H33 cm | H 48 cm |
| H34 cm | H 52 cm |
| H36 cm | H 56 cm |

These formworks are stackable and can be transported and stored in small spaces. They are provided with cone shaped feet with variable height, from 5 to 10 cm and a spacer from 10 a 24 cm .


This peculiarity permits the installation of the elements right on the lower formwork, raising them from the reinforcements.

In this way, the slab che be reinforeced like a normal plate and the pour can be made during just one day.
The realisation times are the same of those of a massive slabs.

### 3.1.2. MODELLING AND STRESS CALCULATION

The overlapping of the plastic blocks created a grid of ribbing, with a variable thickness from 5 to 10 cm .


Figura 3 - A section of a typical lightened slab


Figura 4 -A section of lightened slab with "double"elements


Figura 5 - A section of lightened slab with "single" elements

There are different methods to create these types of structures and obtain the stresses they suffer:

### 3.1.2.1.TIMBER-FRAMED BEAMS MODEL

The structure is similiar to a grid of beams where the section is determine by the type of lightening.
The choice of the section is very important. According to the theory of De Saint Venant, if we decide to set a I section, opened profiles have no torsional stiffness. The bending and shear moment will be sufficiently accurate. The structure will have an higher deformability and the main reason we chose this type of structure will be lost. We will not obtain a slab

In alternative, we can model the grid by setting a rectangular and hollow section. In this way, it is possible to recover the torsional stiffness.

Another method is the modelling of the inverted T shaped beam grid, connected to a slab element equal to the upper hood.

This last method is correct, but there is the risk to lose the advantages of the slab structure. Moreover, the beams should be verified one at a time and this is very time-consuming.

### 3.1.2.2.PLATE MODEL

This is a slab for all intents and purposes. As a reference in the Eurocode 2 says, in chapter 5.3 .1 (6):
"Ribbed or waffle slabs need not be treated as discrete elements for the purposes of analysis, provided that the flange or structural topping and transverse ribs have sufficient torsional stiffness. This may be assumed provided that:

- the depth of the rib below the flange does not exceed 4 times its width.
- the depth of the flange is at least $1 / 10$ of the clear distance between ribs or 50 mm , whichever is the greater.
- transverse ribs are provided at a clear spacing not exceeding 10 times the overall depth of the slab."

These plastic formworks always respects the prescriptions described above, because of their geometry and structure. Therefore, the final result will be a real slab.


Figura 6 - Typical section of a plastic formwork
In the case we use a finite elements calculation, we should anlyze a full slab with the same characteristics of the lightened one.

If, on the other hand, we follow the theory of the orthotropic slab by Kirkhhoff, the following parameters should be taken into consideration:

Flexional stiffness (symmetric in comparison to the two orthogonal directions)

1. Flexional Stiffness
2. Cutting Stiffness

In addition, the slab will be lighter

### 3.1.2.2.1. FLEXIONAL STIFFNESS

According to Kirchhoff the flexional stiffness of a slab is:
$R_{f}=\frac{E \cdot J}{(1-\mu)^{2}}$
E = Elastic Module
$\mathrm{J}=$ Moment of Inertia
$m=$ Poisson's ratio

In the case of a full slab the flexional stiffness will be:
$R_{f}=\frac{E \cdot H^{3}}{(1-\mu)^{2}}$
$\mathrm{H}=$ thickness of the slab


When we obtain the section of the slab embeded in the formwork, we can use Huygens theorem. In this way the Moment of Inertia will be of:
$I^{\prime}=\int_{A} r^{2} \cdot d A$
And the flexional stiffness of the lightness slab:
$R_{f}^{\prime}=\frac{E \cdot J^{\prime}}{(1-\mu)^{2}}$


It will depend on the thickness chosen. The thickness of the upper and lower slabs and of the ribbings will affect the Inertia of the slab. It should be:
$R_{f}=R_{f}^{\prime}$
In order to model a full slab with the same flexional stiffness of the lightened one, it is necessary to reduce the Elastic Module or the Inertia Moment:
$\alpha_{r f}=12 \cdot \frac{J^{\prime}}{i \cdot H^{3}}$
$i=$ Wheelbase of the lightenings $(B+b)$
The model between the Inertia Moments

### 3.1.2.2.2. TORSIONAL STIFFNESS

Even in this case, it is possible to calculate the torsional stiffness of the full section and of the lightened one.

The model is:
$\alpha_{r t}=\frac{J_{t}^{\prime}}{J_{T}}$
It represents the factor of reduction of the torsional stiffness.

### 3.1.2.2.3. CUTTING STIFFNESS

In this case the factor of reduction of stiffness, will be the relationship between the full area and the lightened area:
$\alpha_{t}=\frac{A^{\prime}}{A}$
$A^{\prime}=A_{1}-A_{2}$
It can vary by changing the wheelbase of the lightenings. More specifically, the decrease or increase of the ribbing width.



### 3.1.2.2.4. SELF-WEIGHT CALCULATION

The self-weight of the lightened slab depends on the volume $V$ of the lightening and of the chosen wheelbase. The wheelbase determine the unit impact of the lightenings:
$n=\frac{1}{i^{2}}\left[\mathrm{pc} / \mathrm{m}^{2}\right]$
Concrete consumption of a lightened slab with thickness H (expressed in meters) will be:
$C_{a}=0,01 \cdot H-(n \cdot V)\left[\mathrm{m}^{3} / \mathrm{m}^{2}\right]$
Once again the relationship between this value and value $C_{m}$ of the full slab will reduce the mass of the slab:
$\alpha_{m}=\frac{C_{a}}{C_{m}}$


Figura 7-Calculation of the formworks incidence per square meter

### 3.1.2.2.5. CONSTRUCTION OF THE CALCULATION MODEL

Now, we can model the structure. We need to assign the reduction coefficents to the lightened parts calculated above, while leaving unchanged the parts which will be made in full concrete.

The extension of the capitals over the pillars, can be calculated taking into consideration, as minimal extension the one in the punching perimeter. This can resist without any reinforcement and it is not lower than $2,75 d$ from the edge of the pillar.


Figura 8 - Typical layout of lightenings with massive zones over the pillars


Figura 9-FEM model for lightened slabs- in purple the massive zone, in grey the lightened zones

## DIMENSIONING AND VERIFICATION OF THE REINFORCEMENTS

Once the calculation model is completed, it will be possible to obtain the stress value ( $\mathrm{N}, \mathrm{M}, \mathrm{V}$ ) that acts on the lightened slab.

Then, it is possible to dimension and verify the reinforcement, applying the usual methods of contruction and following the national regulations.

## CHECK TO BENDING

For the check to bending it is possible to use two methods:
Method Wood-Armer: we take into consideration two artificial moments that follow two ortogonal directions, $\mathrm{M}_{\mathrm{xx}}^{*}$ e $\mathrm{M}^{*}{ }_{\mathrm{yy}}$ they are calculated combining the moments adequately $\mathrm{M}_{\mathrm{xx}}$ e $\mathrm{M}_{\mathrm{yy}}$. Usually, finite elements software calculate automatically the moments $M_{x x}^{*}$ e $M^{*}{ }_{y y}$ to use for the calculation of the reinforcements.


Figure 3.5: Rectangular stress distribution



1. Method Hillerborg: known also as stripes method. The slab is divided in strings/beams considered indipendent from one another. Then the reinforcement is dimensioned on the basis of the moments $M_{x x}$ e $M_{y y}$.

Once the moments of stress have been calculated, the dimensioning and check of the reinforcement can be made. The calculation is called break at last limit and it is made taking into consideration the section a lor the section hollow rectangular.

The regulation of Eurocode 2 that need to be followed are the same of full slabs:
6.1 - Simple and compote flexion

- 6.6-Anchoring and overlapping
- 7.3-Cracking management
- 8.1 - Generality
- 8.2 -Space between the reinforcements
- 8.3 - Eligible diameters Mandrels for bent bars
- 8.4 - Anchoring length for the longitudinal reinforcements
- 9.2.1.1 - Minimal section of the reinforcements
- $\quad 9.3 .1$ - Flexion reinforcements (slabs)
- 9.4 -Honeycomb plates


### 3.1.2.3.SHEAR AND PUNCHING CHECK

The lightening reduces the shear section of the slab.
The shear reinforcement needs to be checked in proximity of the massive capitals.


Figure 10 - Punching or reinforcements typical disposition
The shear check will be done while taking into consideration the hollow section of the lightened slab:


According to the hollow section which is wide:
$i=(B+b)$
The reinforcements resistance will be equal to:
$V_{r d, c}=\alpha_{t} \cdot v_{r d} \cdot l \cdot d$
$\alpha_{t}=\frac{A^{\prime}}{A}$ ratio between lightened section's area and full section
$v_{r a, c}=C_{r d, c} \cdot k \cdot\left(100 \cdot \rho_{l} \cdot f_{c k}\right)^{\frac{1}{3}} \geq v_{\text {min }}$ according with EC2 6.6.2
At all points where this value is exceeded, normally close to the capitals and the supports on the sets, you should expect cutting armature, usually vertical pins. The cutting resistance of the section will therefore be the lowest value between
$V_{r d, \text { max }}=\alpha_{t} \cdot \frac{\alpha_{c w} \cdot l \cdot z \cdot v_{1} \cdot f_{c d} \cdot(\cot \theta+\cot \alpha)}{1+\cot ^{2} \alpha}$
And
$V_{r d, s}=\frac{A_{s w}}{s} \cdot z \cdot f_{w y} \cdot(\cot \theta+\cot \alpha) \cdot \sin \alpha$
According with EC2 6.2 .3 (4) expressions 6.13 and 6.14


Figure 11-Example of vertical brackets for cutting effort


Figure 12- Cutting force brackets - Longitudinal section in the rib
As for punching, since massive areas are close to the supports, the normal sizing and checking methods used for massive plates are followed. Additional information is available at the following points in Eurocode 2 :

- 6.2.1 - Cutting effort: general verification procedure
- 6.4.1 - Punching: general
- 8.5 - Anchoring of cutting armatures and other transverse reinforcements
- 9.3.2 - Cutting armatures
- 9.4.3 - Punching armatures


### 1.1.1.1. RETREAT AND FLUAGE

In this case you can easily follow the Eurocode 2 requirements:

- 2.3.2.2 - Retreat and fluage
- 5.8.4 - Fluage
- Annex B -Deformations due to retreat and fluage


### 1.1.1.2. CALCULATION OF INFLESSION AND CHECK OF ARROWS

The calculation of the inflection may be carried out in accordance with the requirements of Chapter 7.4.3 of the Eurocode 2.

Guidelines for checking the arrows are found in Chapter 7.4.
If you want to calculate the finite element arrows with nonlinear analysis, it should be noted that in the cracked phase the lightened slab has the same inertia as the full one only until the neutral axis does not intersect the rib.

It is therefore necessary to check the position of the neutral axis and to apply appropriate inertia modifiers, calculated in the same way as for the elastic section, but on the severed sections.

### 1.1.2. FIRE RESISTANCE

Fire resistance criteria are given in chapter 5.7.5 of EC 2 part 1-2, tables 5.10 and 5.11:

Table 5.10: Minimum dimensions and axis distance for two-way spanning, simply supported ribbed slabs in reinforced or prestressed concrete.

| Standard Fire Resistance | Minimum dimensions ( mm ) |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Possible combinations of width of ribs $b_{\text {min }}$ and axis distance a |  |  | Slab thickness $h_{5}$ and axis distance $a$ in flange |
| 1 | 2 | 3 | 4 | 5 |
| REI 30 | $\begin{aligned} b_{\min } & =80 \\ a & =15^{*} \end{aligned}$ |  |  | $\begin{aligned} h_{\mathrm{s}} & =80 \\ a & =10^{*} \end{aligned}$ |
| REI 60 | $\begin{aligned} b_{\min } & =100 \\ a & =35 \end{aligned}$ | $\begin{aligned} & 120 \\ & 25 \end{aligned}$ | $\begin{gathered} \geq 200 \\ 15^{*} \end{gathered}$ | $\begin{aligned} h_{\mathrm{s}} & =80 \\ a & =10^{*} \end{aligned}$ |
| REI 90 | $\begin{aligned} b_{\min } & =120 \\ a & =45 \end{aligned}$ | $\begin{gathered} 160 \\ 40 \end{gathered}$ | $\begin{gathered} \geq 250 \\ 30 \end{gathered}$ | $\begin{aligned} h_{\mathrm{s}} & =100 \\ a & =15^{*} \end{aligned}$ |
| REI 120 | $\begin{aligned} b_{\min } & =160 \\ a & =60 \end{aligned}$ | $\begin{gathered} 190 \\ 55 \end{gathered}$ | $\begin{gathered} \geq 300 \\ 40 \end{gathered}$ | $\begin{aligned} h_{\mathrm{s}} & =120 \\ a & =20 \end{aligned}$ |
| REI 180 | $\begin{gathered} b_{\min }=220 \\ a=75 \end{gathered}$ | $\begin{gathered} 260 \\ 70 \end{gathered}$ | $\begin{gathered} \geq 410 \\ 60 \end{gathered}$ | $\begin{aligned} h_{\mathrm{s}} & =150 \\ a & =30 \end{aligned}$ |
| REI 240 | $\begin{aligned} b_{\min } & =280 \\ a & =90 \end{aligned}$ | $\begin{gathered} 350 \\ 75 \end{gathered}$ | $\begin{gathered} \geq 500 \\ 70 \end{gathered}$ | $\begin{aligned} h_{\mathrm{s}} & =175 \\ a & =40 \end{aligned}$ |
| $a_{\text {sd }}=a+10$ |  |  |  |  |
| (x) For prestressed ribbed slabs, the axis-distance a should be increased in accordance with 5.2(5). $x$ <br> $a_{\text {sd }}$ denotes the distance measured between the axis of the reinforcement and lateral surface of the rib exposed to fire. |  |  |  |  |
| * Normally the cover required by EN 1992-1-1 will control. |  |  |  |  |



Alternatively, it is possible to conduct an analytical calculation to the finite elements using a standard temperature curve according to the requirements of chapter 4.3 of EC2 part 1-2.

### 1.1.3. ACOUSTIC PERFORM ANCE

Normally lightening suppliers provide on-demand laboratory or on-site testing of the acoustic performance of the construction system, based on which you can estimate the slab performance you are designing.

### 1.1.4. CONCRETE CASTING M ETHODOLOGY

The lightening caissons are watertight, as the air clamped inside them prevents the entrance of the concrete.

For this reason they tend to float during the casting, developing a vertical force such that it is possible to lift the upper armature.

The cast has to be run in two phases, both in the same day: a first strut of the lift leg, then the completion layer, to be performed after 2-4 hours (depending on the outside temperature).

In case the cast is run several hours later, it is necessary to calculate and provide a suitable shot armor.


Figure 13 - Cast of the first layer


Figure 14-Cast of the completion layer

### 1.2. COM PARISON WITH THE FULL PLATES

Lightened plates retain all the features and benefits of their massive structures:

1. Thicknesses reduced
2. No beams
3. High rigidity and reduced arrows
4. Good fire behavior
5. Ease of operation thanks to the use of basically straight bars and electrowelded nets for the armor.

Obviously, the reduction of material obtained through the interposition of lightening in the casting results in a reduction of the rigidity of the structure, but is compensated by the greater lightness.

### 1.2.1. PREDIM ENSIONING

As for the first predimensioning of the thickness, lightened plates follow the same criteria and practical rules normally used for full plates:

1. Lightened plate on pillars: $\mathrm{L} / 25<S<L / 30$ depending on the ELU load
2. Lightened plate on lowered beams or capitals: $\mathrm{L} / 30<\mathrm{S}<\mathrm{L} / 35$

Below is a table that provides an idea of the predimensioning of a lightened plate according to the span between the pillars and in the case of a load $\mathrm{G}^{\prime}{ }_{k}+\mathrm{Q}_{\mathrm{k}}=5,0 \mathrm{kN} / \mathrm{m}^{2}$


| $\begin{aligned} & \text { SPAN } \\ & \text { S } \\ & \text { SPACI } \\ & \text { NG } L_{x} \\ & \mathrm{x} \mathrm{~L}_{\mathrm{y}} \end{aligned}$ | $\begin{aligned} & \text { LOAD } \\ & \text { S G }_{k}^{\prime} \\ & +\mathrm{Q}_{\mathrm{k}} \end{aligned}$ | PROPOSED THICKNESS | $\mathrm{S}_{1}$ | $\begin{gathered} \mathbf{H}_{\text {naut }} \\ \text { ifus } \end{gathered}$ | $\mathrm{S}_{2}$ | INERTIA NAUTIL US SLAB Jnau | $\begin{aligned} & \text { INER } \\ & \text { TIA } \\ & \text { FLAT } \\ & \text { SLAB } \\ & \text { Jfull } \end{aligned}$ | SELF WEIGHT NAUTILUS SLAB $\mathrm{P}_{\text {nau }}$ | $\begin{aligned} & \text { SELF } \\ & \text { WEIG } \\ & \text { HT } \\ & \text { FLAT } \\ & \text { SLAB } \\ & \text { P fill }^{2} \end{aligned}$ | $\begin{aligned} & \text { INER } \\ & \text { TIA } \\ & \text { LOSS } \end{aligned}$ | WEIGHT/ CONCRETE REDUCTION | LOADS/REINFOR CEMENT REDUCTION |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| [m] | $\begin{gathered} {[\mathrm{kN} /} \\ \left.\mathrm{m}^{2}\right] \end{gathered}$ | [cm] | $\begin{gathered} {[\mathrm{c}} \\ \mathrm{m}] \end{gathered}$ | [cm] | $\begin{aligned} & \text { [c } \\ & \mathrm{m}] \end{aligned}$ | [ $\mathrm{cm}^{4}$ ] | $\left[\mathrm{cm}^{4}\right]$ | [ $\mathrm{kN} / \mathrm{m}^{2}$ ] | $\begin{gathered} {[\mathrm{kN} /} \\ \left.\mathrm{m}^{2}\right] \end{gathered}$ | \% | \% | \% |
| 5 | 5.00 | 20 | 5 | 10 | 5 | $\begin{gathered} 60821.2 \\ 6 \end{gathered}$ | $\begin{aligned} & 6666 \\ & 6.67 \end{aligned}$ | 3.63 | 5.00 | $\begin{gathered} 8.77 \\ \% \end{gathered}$ | -27.4 | -13.0 |
| 6 | 5.00 | 23 | 5 | 13 | 5 | $\begin{gathered} 88537.9 \\ 5 \end{gathered}$ | $\begin{aligned} & 1013 \\ & 91.67 \end{aligned}$ | 4.15 | 5.75 | $\begin{gathered} 12.68 \\ \% \end{gathered}$ | -27.8 | -14.2 |
| 7 | 5.00 | 25 | 6 | 13 | 6 | $117362 .$ | $\begin{gathered} 1302 \\ 08.33 \end{gathered}$ | 4.65 | 6.25 | $\begin{gathered} 9.87 \\ \% \end{gathered}$ | -25.6 | -13.6 |
| 8 | 5.00 | 28 | 6 | 16 | 6 | $\begin{gathered} 158952 . \\ 73 \end{gathered}$ | $\begin{aligned} & 1829 \\ & 33.33 \end{aligned}$ | 5.18 | 7.00 | $\begin{gathered} 13.11 \\ \% \end{gathered}$ | -26.0 | -14.5 |
| 9 | 5.00 | 32 | 7 | 20 | 5 | $\begin{gathered} 226197 . \\ 71 \end{gathered}$ | $\begin{gathered} 2730 \\ 66.67 \end{gathered}$ | 5.78 | 8.00 | $\begin{gathered} 17.16 \\ \% \end{gathered}$ | -27.8 | -16.4 |
| 10 | 5.00 | 34 | 7 | 20 | 7 | $\begin{gathered} 280664 . \\ 38 \end{gathered}$ | $\begin{aligned} & 3275 \\ & 33.33 \end{aligned}$ | 6.28 | 8.50 | $\begin{gathered} 14.31 \\ \% \end{gathered}$ | -26.1 | -15.8 |
| 11 | 5.00 | 36 | 7 | 24 | 5 | $\begin{gathered} 307772 . \\ 12 \end{gathered}$ | $\begin{aligned} & 3888 \\ & 00.00 \end{aligned}$ | 6.38 | 9.00 | $\begin{gathered} 20.84 \\ \% \end{gathered}$ | -29.1 | -18.0 |
| 12 | 5.00 | 40 | 8 | 24 | 8 | $\begin{gathered} 452305 . \\ 45 \end{gathered}$ | $\begin{aligned} & 5333 \\ & 33.33 \end{aligned}$ | 7.38 | 10.00 | $\begin{gathered} - \\ 15.19 \\ \% \end{gathered}$ | -26.2 | -16.8 |
| 13 | 5.00 | 44 | 8 | 28 | 8 | $\begin{gathered} 581150 . \\ 55 \end{gathered}$ | $\begin{aligned} & 7098 \\ & 66.67 \end{aligned}$ | 7.98 | 11.00 | $\begin{gathered} 18.13 \\ \% \end{gathered}$ | -27.5 | -18.2 |
| 14 | 5.00 | 50 | 7 | 36 | 7 | $\begin{gathered} 779649 . \\ 39 \end{gathered}$ | $\begin{gathered} 1041 \\ 666.6 \\ 7 \end{gathered}$ | 8.48 | 12.50 | $\begin{gathered} 25.15 \\ \% \end{gathered}$ | -32.2 | -22.3 |
| 15* | 5.00 | 58 | 10 | 41 | 7 | $\begin{gathered} 123641 \\ 3.18 \end{gathered}$ | $\begin{gathered} 1625 \\ 933.3 \\ 3 \end{gathered}$ | 9.98 | 14.50 | $\begin{gathered} 23.96 \\ \% \end{gathered}$ | -31.2 | -22.5 |
| 16* | 5.00 | 64 | 8 | 48 | 8 | $\begin{gathered} 156185 \\ 1.26 \end{gathered}$ | $\begin{gathered} 2184 \\ 533.3 \\ 3 \end{gathered}$ | 10.73 | 16.00 | $\begin{gathered} 28.50 \\ \% \end{gathered}$ | -32.9 | -24.4 |
| 17** | 5.00 | 68 | 10 | 48 | 10 | $\begin{gathered} 199758 \\ 4.59 \end{gathered}$ | $\begin{gathered} 2620 \\ 266.6 \\ 7 \end{gathered}$ | 11.73 | 17.00 | $\begin{gathered} 23.76 \\ \% \end{gathered}$ | -31.0 | -23.4 |
| 18** | 5.00 | 72 | 10 | 52 | 10 | $\begin{gathered} 231796 \\ 2.12 \end{gathered}$ | $\begin{gathered} 3110 \\ 400.0 \\ 0 \end{gathered}$ | 12.43 | 18.00 | $25.48$ \% | -30.9 | -23.6 |


| 19** | 5.00 | 74 | 10 | 56 | 8 | $\begin{gathered} 238673 \\ 9.39 \end{gathered}$ | $\begin{gathered} 3376 \\ 866.6 \\ 7 \end{gathered}$ | 12.65 | 18.50 | $\begin{gathered} 29.32 \\ \% \end{gathered}$ | -31.6 | -24.3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 20** | 5.00 | 76 | 10 | 56 | 10 | $\begin{gathered} 266800 \\ 6.06 \end{gathered}$ | $\begin{gathered} 3658 \\ 133.3 \\ 3 \end{gathered}$ | 13.15 | 19.00 | $\begin{gathered} 27.07 \\ \% \end{gathered}$ | -30.8 | -23.8 |

*High performances concrete reccomended - ** Post tensioning reccomended

### 1.2.2. EFFECTS OF THE REDUCTION OF STIFFNESS

Reduction of rigidity is a function of the lightening geometry and is not linear with its height, it is also influenced by the thickness of the lower plate and, to a lesser extent, by the distance between the lightenings.

It is important to calibrate the lightened section so that the stiffness reduction is compensated by the lightness of the plate, calibrating the thicknesses of the slabs.

The following charts show how, when the height of the lightening and therefore the thickness of the plate is altered, and a distance is fixed, by increasing the thickness of the hoods, it is always possible to make the weight reduction superior to the loss of stiffness, thus keeping the performance of the lightened plate unaltered with respect to the full equivalent.


Graph 1-Loss of flexural strength Vs. Weight reduction for lightweight plates with top and bottom 5 cm thickness


Graph 2 - Loss of flexural strength Vs. Weight reduction for lightweight plates with top and bottom 7 cm thickness


Graph 3-Loss of flexural strength Vs. Weight reduction for lightweight plates with top and bottom 10 cm thickness

### 1.2.2.1. CONCLUSIONS

If you dimension the section appropriately, choosing the lightening height depending on the desired thickness and the appropriate thickness of the upper and lower plates, it is always possible to ensure that the loss of inertia is clearly compensated by the weight reduction.

By doing this, plates are obtained which have an average weight of $25 \%$ less than the full equivalent, losing only an 8-15\% stiffness.

### 1.2.3. STRESSING LOAD REDUCTION

The first consequence of weight reduction of the same thickness as the homogeneous mass plate is that the slab and vertical structures all benefit from a reduction in load to the ultimate state which is the function of decreasing the proper weight of the plate and the size of the loads of the project.

The following graphs show that, as the thickness of the upper and lower plates varies, the vertical load reduction to the Ultimate Limit State is variable from 8 to $10 \%$ minimum, up to $25 \%$.

The graphs show the magnitude of the benefit in the case of a fixed $G_{k}$ permanent load of $2,0 \mathrm{kN} / \mathrm{m}^{2}$ at the variation of the plate thickness and variable load $\mathrm{Q}_{\mathrm{k}}$. Also the width of the rib is assumed invariable.

The vertical load reduction allows for direct savings of reinforcing steel in the slab, but also indirect savings on sizing of pillars. This savings helps to further lighten the entire structure, resulting in benefits to the foundation structures.


Graph 4 - ELU Load reduction depending on the thickness of the slab in the case of bottom and top plates of 5 cm thickness


Graph 5 - ELU Load reduction depending on the thickness of the slab in the case of bottom and top plates of 7 cm thickness


Graph 6-ELU Load reduction depending on the thickness of the slab in the case of bottom and top plates of 10 cm thickness

### 1.2.4. SEISM IC M ASS REDUCTION

Lightening the slabs and consequently the entire structure has important consequences on the seismic behavior of the structure.

Although it is not possible to give generic indications of the extent of the benefits on the seismic level as seismic acceleration is given by the response spectrum curve which is the function of the particular vibration period of the structure, which must be assessed case by case, it remains undeniable that the active seismic force is a direct function of the mass of the building.

The lightening of the slabs and consequently of the vertical structures therefore results in a significant reduction of the seismic force acting on the building.

### 1.2.5. COM PARISON ON TYPE BUILDINGS

By way of example we have made a comparison between two identical buildings, one with massive slabs and one with lightweight slabs.

The starting hypotheses are the following:

1. Slabs 28 cm thick and with a surface of about $500 \mathrm{~m}^{2}$
2. Span between pillars $8 \times 8 \mathrm{~m}$
3. 10 storey building
4. Pillars automatically dimensioned by FEM software to appreciate load savings on the verticals
5. Project loads: $G_{k}=2,0 \mathrm{kN} / \mathrm{m}^{2}-Q_{k}=3,0 \mathrm{kN} / \mathrm{m}^{2}$
6. Seismic acceleration peak at reference ground: $0,257 \mathrm{~g}$


Figure 15 - Plant of lightweight slab type


Figure 16 - Building calculation model

|  |  | FUIL PLATE | LICHTENED PLATE |
| :---: | :---: | :---: | :---: |
| TOTAL THICKNESS | H [mm] | 280 | 280 |
| THICKNESS LOWER PIATE | $\mathrm{S}_{1}[\mathrm{~mm}]$ |  | 60 |
| THICKNESS UPPER PLATE | S2[mm] |  | 60 |
| LGHTENING HEIGHT | H [mm] |  | 160 |
| RIB WIDTH | B [mm] |  | 140 |
| DISTANCE | 1 [mm] |  | 660 |
| SLAB INERTIA | $\mathrm{J}\left[\mathrm{cm}^{4} / \mathrm{m}\right]$ | 182.933 | 158.844 |
| CONCREIE CONSUMPTION | $\mathrm{C}\left[\mathrm{m}^{3} / \mathrm{m}^{2}\right]$ | 0.280 | 0.207 |
| OWN WEGHT | $\mathrm{P}\left[\mathrm{kN} / \mathrm{m}^{2}\right]$ | 7,0 | 5,18 |



Figure 1 - FEM model of the type plate

1. In dark grey: shaped plate as lightened
a. Bending flexibility reduction factor: 0,87
b. Cutting stiffness reduction factor: 0,60
c. Mass reduction factor: 0,74
2. In light grey: shaped plate as full
a. Bending flexibility reduction factor: 1,00
b. Cutting stiffness reduction factor: 1,00
c. M ass reduction factor: 1,00

### 1.2.6. COM PARISON OF THE DEFORM ED




Figure 2-Long-term arrow: $49,76 \mathrm{~mm}$


Figure 3 - Long-term arrow: 42,77

### 1.2.7. COM PARISON OF BENDING M OM ENTS



Figure 4 - Full plate - Mxx



Figure 4 - Full plate: Myy


Figure 5 - Lightened plate: Myy

### 1.2.8. CONCLUSIONS

|  | FULL | LIGHTENED | DIFF. \% |
| :--- | :--- | :--- | :--- | :--- |
| ARROW $[\mathrm{mm}]$ | 49.76 | 42.77 | $-14 \%$ |


|  |  | FULL | LIGHTENED | DIFF. \% |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{M}_{\mathrm{xx}}{ }^{+}$ | $[\mathrm{kNm}]$ | 115.02 | 73.56 | $-36.05 \%$ |
| $\mathrm{M}_{\mathrm{xx}}{ }^{-}$ | $[\mathrm{kNm}]$ | -425.06 | -229.75 | $-45.95 \%$ |
| $\mathrm{M}_{\mathrm{yy}}{ }^{+}$ | $[\mathrm{kNm}]$ | 91.84 | 98.87 | $7.65 \%$ |
| $\mathrm{M}_{\mathrm{yy}}{ }^{-}$ | $[\mathrm{kNm}]$ | -346.82 | -287.99 | $-16.96 \%$ |

Bending moments obviously result from redistribution due to the fact that the full plate has constant stiffness while the lightened is more rigid to the supports, thus resulting in a negative moment migration.

The average reduction of bending moment is around $17 \%$.

### 1.2.9. OVERALL LOAD REDUCTION

If we go to evaluate the weight and load reduction of each slab, added to the weight reduction due to the optimization of vertical structures subject to lower load, the overall benefit is even greater than not simply on the slab:

## PLEINE

| Load Case/Combo |  | Load Case/Combo |  |
| :---: | :---: | :---: | :---: |
|  | F7 |  | 「Z |
|  | kN |  | kN |
| Poids propre | 45007 | Poids propre | 30464 |
| Utile | 13627 | Utile | 13627 |
| Perm. | 9084 | Perm. | 9084 |
| ELU | 93586 | ELU | 73831 |

1. $-26 \%$ on the weight of the slabs
2. $-32 \%$ of the total building weight
3. $-21 \%$ of global load in foundation

### 1.2.10. REDUCTION OF SEISM IC LOAD

We made a comparison between the two buildings also from the seismic point of view, taking as reference the curve of the response spectrum of the Italian standard, in a highly seismic zone and in the pessimistic hypothesis of a type $D$ soil.


The tables below show the different modal participation masses in the case of a building with a full or allround plate:


| FULL |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Case | Mode | Period sec | UX | UY | UL | Sum UX | Sum UY |
| Modal | 1 | 0.83 | 0.50 | 0.00 | 0.00 | 0.50 | 0.00 |
| Modal | 2 | 0.48 | 0.00 | 0.63 | 0.00 | 0.50 | 0.68 |
| Model | 3 | 0.34 | 0.15 | 0.00 | 0.00 | 0.66 | 0.68 |
| Modal | 4 | 0.22 | 0.15 | 0.00 | 0.00 | 0.80 | 0.68 |
| Modal | 5 | 0.11 | 0.01 | 0.11 | 0.00 | 0.81 | 0.79 |
| Modal | 6 | 0.11 | 0.01 | 0.10 | 0.00 | 0.83 | 0.89 |
| Modal | 7 | 0.08 | 0.08 | 0.00 | 0.00 | 0.91 | 0.89 |
| Modal | 8 | 007 | 002 | 000 | 000 | 0.93 | 089 |
| Modal | 9 | 0.05 | 0.01 | 0.00 | 0.00 | 0.94 | 0.89 |
| Modal | 10 | 0.05 | 0.00 | 0.03 | 0.00 | 0.94 | 0.95 |
| Modal | 11 | 0.04 | 0.00 | 0.00 | 0.00 | 0.94 | 0.95 |
| Modal | 12 | 0.04 | 0.03 | 0.00 | 0.00 | 0.97 | 0.95 |
| Modal | 13 | 0.04 | 0.00 | 0.00 | 0.00 | 0.97 | 0.95 |


| VOIDED |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Case | Mode | Period scc | UX | UY | UZ | Sum LIX | Sum UY |
| Modal | 1 | 0.732 | 0.19 | 0.00 | 0.00 | 0.49 | 0.00 |
| Modal | 2 | 0.419 | 0.00 | 0.68 | 0.00 | 0.49 | 0.68 |
| Modial | 3 | 0.306 | 0.17 | 0.00 | 0.00 | 0.66 | 0.68 |
| Modal | 4 | 0.192 | 0.14 | 0.00 | 0.00 | 0.80 | 0.68 |
| Modal | 5 | 0.098 | 0.00 | 0.15 | 0.00 | 0.80 | 0.83 |
| Modal | 6 | 0.093 | 0.02 | 0.05 | 0.00 | 0.82 | 0.89 |
| Modal | 1 | U.0/3 | 0.09 | 0.00 | u.00 | U. 91 | U. 89 |
| Modal | 8 | ¢ 06 | 0.02 | 000 | 000 | 0.93 | 089 |
| Modal | 9 | 0.044 | 0.01 | 0.02 | 0.00 | 0.93 | 0.91 |
| Modal | 10 | 0.044 | 0.00 | 0.04 | 0.00 | 0.93 | 0.95 |
| Modal | 11 | 0.036 | 0.00 | 0.00 | 0.00 | 0.93 | 0.05 |
| Modal | 12 | 0.034 | 0.03 | 0.00 | 0.00 | 0.91 | 0.95 |
| Modal | 13 | 003 | 000 | 000 | 000 | 097 | 0.95 |

The building with full plates has a slightly longer vibration period, while the lightweight slab building is located on the plateau of the curve:


However, the reduction of global mass plays a much more relevant effect on the resulting seismic force:


Figure 6 - Displacement due to seismic forces - full plate building


Figure 7 - Displacement due to seismic forces - lightweight building

The displacement is $36 \%$ lower in case of lightweight slabs.

### 1.2.10.1. REDUCTION OF SEISM IC STRESSES



|  | Combo | Location | FULL |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| story |  |  | vx | Vr | T | MX | MY |
|  |  |  | kN | kN | kN -m | kN -m | kN |
| Story10 | SISM ENV Max | To | 6624 | 8491 | 131852 | 0 |  |
| Story10 | SISM ENV Max | Bottom | 6624 | 8491 | 131852 | 26324 | 20534 |
| Story9 | SISM ENV Max | Top | 12362 | 16163 | 252730 | 26324 | 20534 |
| Story9 | SISM ENV Max | Bottom | 12362 | 16163 | 252730 | 76339 | 58755 |
| Story8 | SISM ENV Max | Top | 16931 | 22274 | 349612 | 76339 | 58755 |
| Story8 | SISM ENV Max | Bottom | 16931 | 22274 | 349612 | 144945 | 110856 |
| Story7 | SISM ENV Max | Top | 20760 | 27247 | 429263 | 144945 | 110856 |
| Slury? | SISM ENV Max | Butlori | 20760 | 27247 | 429263 | 228241 | 173971 |
| Story6 | SISM ENV Max | Top | 24216 | 31379 | 495901 | 228241 | 173971 |
| Story 6 | SISM ENV Max | Bottom | 24216 | 31379 | 495901 | 323377 | 246246 |
| Story | SISM ENV Max | Top | 27037 | 34762 | 550577 | 323377 | 246246 |
| Story | SISM ENV Max | Bottom | 27037 | 34762 | 550577 | 428035 | 326638 |
| Story 4 | SISM ENV Max | Top | 29229 | 37455 | 594336 | 428035 | 326638 |
| Story 4 | SISM ENV Max | Bottom | 29229 | 37455 | 594336 | 540161 | 413830 |
| Story | SISM ENV Max | Top | 30919 | 30516 | 627928 | 540161 | 413830 |
| Story 3 | SISM ENV Max | Bottom | 30919 | 39516 | 627928 | 657940 | 505905 |
| Story2 | SISM ENV Max | Top | 32153 | 40886 | 650204 | 657940 | 505905 |
| Story2 | SISM ENV Max | Bottom | 32153 | 10886 | 650201 | 775759 | 598300 |
| Story1 | SISM ENV Max | Top | 32774 | 41511 | 660294 | 775759 | 598300 |
| Story1 | SISM ENV Max | Bottom | 32774 | 41511 | 660294 | 899933 | 696001 |

## VOIDED

| Story | Combo | Location | vx | VY | T | MX | Mr |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | kN | kN | kN-m | kN-m | kN-m |
| Story10 | SISM ENV Max | Top | 3589 | 5271 | 83905 | 0 | 0 |
| Story10 | SISM ENV Max | Bottom | 3589 | 5271 | 83905 | 16340 | 12365 |
| Stury ${ }^{\text {a }}$ | SISM ENV Max | Top | 7746 | 10369 | 167271 | 16340 | 12365 |
| Story 9 | SISM ENV Max | Bottom | 7746 | 10369 | 167271 | 48425 | 36311 |
| Story 8 | SISM ENV Max | Top | 10809 | 11113 | 231219 | 18125 | 36311 |
| Story8 | SISM ENV Max | Bottom | 10809 | 14443 | 234249 | 92912 | 69569 |
| Story7 | SISM ENV Max | Top | 13373 | 17759 | 289053 | 92912 | 69569 |
| Story7 | SISM ENV Max | Bottom | 13373 | 17759 | 289053 | 147222 | 110371 |
| Story6 | SISM ENV Max | Top | 15537 | 20509 | 334565 | 147222 | 110371 |
| Story6 | SISM ENV Max | Bottom | 15537 | 20509 | 334565 | 209460 | 157446 |
| Story 5 | SISM ENV Max | Top | 17309 | 22759 | 371808 | 209460 | 157446 |
| Story 5 | SISM ENV Max | Bottom | 17309 | 22759 | 371808 | 278086 | 209054 |
| Story 4 | SISM ENV Max | Top | 18749 | 24546 | 401687 | 278086 | 209654 |
| Story 4 | SISM ENV Max | Bottom | 18749 | 24546 | 401087 | 351718 | 265888 |
| Story 3 | SISM ENV Max | Top | 19872 | 25909 | 424734 | 351718 | 265888 |
| Story 3 | SISM ENV Max | Bottom | 19872 | 25909 | 424734 | 429115 | 325172 |
| Story2 | SISM ENV Max | Top | 20638 | 26818 | 440092 | 429115 | 325172 |
| Story2 | SISM ENV Max | Bottom | 20638 | 26818 | 440092 | 506547 | 384614 |
| Story1 | SISM ENV Max | Iop | 21004 | 21235 | 44/J49 | 30654/ | 384614 |
| Story1 | SISM ENV Max | Bottom | 21004 | 27235 | 447049 | 588138 | 447342 |



Figure 26 - Horizontal seismic force per plane - direct. X


Figure 27-Horizontal seismic force per plane - direct. Y

Even in this case, the reduction of the soliciting force is important and in the order of $36 \%$ less.

### 1.2.11. CONCLUSIONS

To lighten the plates of a building has as immediate impact on the steel reduction of armor on the plates themselves, that we have seen to be average in the 12-15 order\%.

Greater lightness also reduces the overall weight of the building as horizontal structures can be reduced due to the increased lightness of the slabs.

The benefit obviously grows as the number of floors in the building increases, and can lead to a reduction in the overall building weight of $30 \%$ and a reduction in the foundation load by $20 \%$.

Similarly, the seismic forces decrease significantly, in the case example, a $36 \%$ less.
It remains to assess the burden of buying lightening and putting them into operation.
Depending on the cost of concrete, which varies not only from nation to nation, but also from region to region or city to city (especially in large urban centers it is usually much more expensive due to logistical burdens), the impact of the lightening on the cost of the lightened plate is greater or lesser.

On average, the cost of the lightening is largely offset by the savings of concrete generated by it, the remainder being largely compensated by the steel savings that are obtained on the totality of the building.

The time and consequent cost of laying workmanship is rather reduced ( $30-40 \mathrm{~m}^{2} / \mathrm{h}$ per worker) and is largely offset by the fact that saving steel on the slabs reduces the laying time of the same, and that time can be used for laying the lightening.

This implies that the productivity of a lightened plate is also the same as a full plate.

